**Assignment 3 – Recursion**

*Write pseudo-code for problems requiring code. Do not write Java, Python or C++. You are responsible for the appropriate level of detail. For the questions asking for justification, please provide a detailed mathematically oriented discussion. A proof is not required.*

*Q1 and Q2 are intended to help you get comfortable with recursion by thinking about something familiar in a recursive manner. Q3 – Q6 are practice in working with non-trivial recursive functions. Q7 deals with the idea of conversion between iteration and recursion.*

**1. Write a recursive algorithm to compute *a+b*, where *a* and *b* are nonnegative integers.**

**2. Let A be an array of integers. Write a recursive algorithm to compute the average of the elements of the array.** Solutions calculating the sum recursively, instead of the average, are worth fewer points.

**3. If an array contains n elements, what is the maximum number of recursive calls made by the binary search algorithm?**

**4. The expression m % n yields the remainder of m upon (integer) division by n. Define the greatest common divisor (GCD) of two integers x and y by:**

**gcd(x, y) = y if ( y ≤ x and x%y == 0)**

**gcd(x, y) = gcd(y, x) if (x < y )**

**gcd(x, y) = gcd(y, x%y) otherwise**

**Write a recursive method to compute gcd(x,y).**

**5. A generalized Fibonacci function is like the standard Fibonacci function,, except that the starting points are passed in as parameters. Define the generalized Fibonacci sequence of f0 and f1 as the sequence gfib( f0, f1, 0), gfib(f0, f1, 1), gfib(f0, f1, 2), ..., where**

**gfib(f0, f1, 0) = f0**

**gfib(f0, f1, 1) = f1**

**gfib(f0, f1, n) = gfib(f0, f1, n-1) + gfib(f0, f1, n-2) if n> 1**

**Write a recursive method to compute gfib(f0,f1,n).**

**6. Ackerman's function is defined recursively on the nonnegative integers as follows:**

a(m, n) = n + 1 if m = 0

a(m, n) = a(m-1, 1) if m ≠ 0, n = 0

a(m, n) = a(m-1, a(m, n-1)) if m ≠ 0, n ≠ 0

Using the above definition, show that a(2,2) equals 7.

**7. Convert the following recursive program scheme into an iterative version that does not use a stack. *f(n)* is a method that returns TRUE or FALSE based on the value of n, and *g(n)* is a method that returns a value of the same type as *n* (without modifying *n* itself).**

int rec(int n)

{

if ( f(n) == FALSE ) {

/\* any group of statements that do not change the value of n \*/

return (rec(g(n)));

}//end if

return (0);

}//end rec